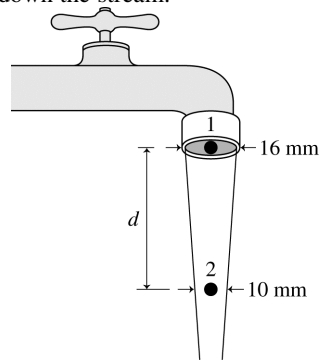


15.62. Model: Treat the water as an ideal fluid obeying Bernoulli's equation. A streamline begins at the faucet and continues down the stream.

Visualize:



The pressure at point 1 is p_1 and the pressure at point 2 is p_2 . Both p_1 and p_2 are atmospheric pressure. The velocity and the area at point 1 are v_1 and A_1 and they are v_2 and A_2 at point 2. Let the distance of point 2 below point 1 be d .

Solve: Bernoulli's equation at points 1 and 2 is

$$p_1 + \frac{1}{2}\rho v_1^2 + \rho g y_1 = p_2 + \frac{1}{2}\rho v_2^2 + \rho g y_2 \Rightarrow \rho g d = \frac{1}{2}\rho(v_2^2 - v_1^2)$$

From the continuity equation,

$$v_1 A_1 = v_2 A_2 \Rightarrow (1.0 \text{ m/s})\pi(8.0 \times 10^{-3} \text{ m})^2 = v_2 \pi(5.0 \times 10^{-3} \text{ m})^2 \Rightarrow v_2 = 2.56 \text{ m/s}$$

Going back to Bernoulli's equation, we have

$$g d = \frac{1}{2}[(2.56 \text{ m/s})^2 - (1.0 \text{ m/s})^2] \Rightarrow d = 0.283 \text{ m} = 28.3 \text{ cm}$$